

Both GCF and Split the middle term

$$4x^2 - 2x - 20$$

$$-3x^2 + 12x + 15$$

$$8x^2 - 28x - 60$$

$$12x^2 + 10x - 8$$

$$112x^2 - 168x + 63$$

Special Cases

Difference of squares

$$a^2 - b^2$$

$$x^2 - 25$$

$$(x-5)(x+5)$$

$$x^2 - 49$$

$$(x+7)(x-7)$$

$$(a-b)(a+b)$$

$$4x^2 - 9$$

$$(2x+3)(2x-3)$$

$$9x^2 - 1$$

$$(3x-1)(3x+1)$$

Solving

1st factor

2nd Set linear factors equal to zero

3rd Solve each linear equation

$$a \cdot b = 0$$

$$(-1)^2 - 3(-1) - 4$$

$$\begin{array}{r} 1 \\ + 3 \\ \hline 4 \end{array}$$
$$x^2 - 3x - 4 = 0$$

$$(x-4)(x+1) = 0$$

$$\begin{array}{l} x-4=0 \\ x+1=0 \end{array}$$

$$\begin{array}{l} x=4 \\ x=-1 \end{array}$$

$$x^2 + 2x - 35 = 0$$

$$(x-5)(x+7) = 0$$

$$x-5=0$$

$$\begin{array}{l} x=5 \\ x=-7 \end{array}$$

$$\frac{20}{-10-5}$$

$$5x^2 - 13x + 6 = 0$$

$$(5x^2 - 10x) + (3x + 6) = 0$$

$$5x(x-2) - 3(x-2) = 0$$

$$(5x-3)(x-2) = 0$$

$$\begin{array}{l} 5x-3=0 \\ x-2=0 \end{array}$$

$$5x = 3$$

$$\begin{array}{l} x=2 \\ x=\frac{3}{5} \end{array}$$

$$\underline{-3x^2 + 3x + 90 = 0}$$

$$\underline{-3} \quad \underline{-3}$$

$$x^2 - x - 30 = 0$$

$$(x-6)(x+5) = 0$$

$$\begin{array}{l} x=6 \\ x=-5 \end{array}$$

$$8x^2 - 6x - 5 = 0$$

$$(4x-5)(2x+1) = 0$$

$$4x-5=0 \quad 2x+1=0$$

$$\begin{array}{l} x=\frac{5}{4} \\ x=-\frac{1}{2} \end{array}$$

$$x^2 + 7x = 0$$

$$x(x+7) = 0$$

$$\begin{array}{l} x=0 \\ x=-7 \end{array}$$

$$5x^2 - 25 = 4x^2 + 24$$

$$\begin{array}{r} 5x^2 \\ - 4x^2 \\ \hline 1x^2 \end{array}$$

$$x^2 - 25 = 24$$

$$2x^2 + 4x - 1 = 7x^2 - 7x + 1$$

$$0 = 5x^2 - 11x + 2$$

$$x^2 - 49 = 0$$

$$= (5x-1)(x-2)$$

$$(x-7)(x+7) = 0$$

$$5x-1=0 \quad x-2=0$$

$$\begin{array}{l} x=7 \\ x=-7 \end{array}$$

$$\begin{array}{l} 5x=1 \\ x=2 \end{array}$$

$$x = \pm 7$$

$$x = \frac{1}{5}$$

$$16x^2 = 8x - 1$$

$$16x^2 - 8x + 1 = 0$$

$$(16x^2 - 4x)(4x + 1) = 0$$

$$4x(4x-1) - 1(4x-1)$$

$$(4x-1)(4x-1) = 0$$

$$x = \frac{1}{4}$$

$$\frac{6x^2 - 10x - 4}{2} = 0$$

$$3x^2 - 5x - 2 = 0$$

$$(3x+1)(x-2) = 0$$

$$3x+1=0 \quad x-2=0$$

$$x = -\frac{1}{3}$$

$$x = 2$$

Solve by taking the Square Root

1. Solve each quadratic by taking the square root.

a. $x^2 = 25$

b. $x^2 = 12$

c. $5x^2 = 75$

d. $5x^2 + 8 = 8$

e. $5x^2 + 15 = 60$

f. $5x^2 + 75 = 60$

g. $-5x^2 + 75 = 60$

2. Solve by factoring

a. $0 = x^2 + 4x$
 $0 = x(x+4)$
 $x=0 \quad x=-4$

b. $0 = 3x^2 + 10x$
 $x(3x+10) = 0$
 $x=0 \quad 3x+10=0$
 $x=-10/3$

c. $-x^2 - 5x = 0$
 $-x(x+5) = 0$
 $x=0 \quad x=-5$

d. $-2x^2 + 6x = 0$
 $-2x(x-3) = 0$
 $x=0 \quad x=3$

e. $x^2 - 7x + 10 = 0$
 $(x-5)(x-2) = 0$
 $x=5 \quad x=2$

f. $x^2 + 12x + 32 = 0$
 $(x+4)(x+8) = 0$
 $x=-4 \quad x=-8$

g. $\frac{2x^2 - 18x - 72}{2} = 0$
 $x^2 - 9x - 36 = 0$
 $(x-12)(x+3) = 0$
 $x=12 \quad x=-3$

h. $x^2 + 5x - 6 = 0$
 $x^2 + 5x - 6 = 0$
 $(x+6)(x-1) = 0$
 $x=-6 \quad x=1$

$$\begin{aligned} j. \quad x^2 - 81 &= 0 \\ (x+9)(x-9) &= 0 \\ x &= \pm 9 \end{aligned}$$

$$\begin{aligned} k. \quad \frac{3x^2 - 27}{3} &= 0 \\ x^2 - 9 &= 0 \\ (x+3)(x-3) &= 0 \\ x &= \pm 3 \end{aligned}$$

$$\begin{aligned} l. \quad 16x^2 - 121 &= 0 \\ (4x+11)(4x-11) &= 0 \\ x &= \pm \frac{11}{4} \end{aligned}$$

$$\begin{aligned} 3x^2 - 5x - 2 &= 0 \\ (3x^2 - 6x) + (x - 2) &= 0 \\ 3x(x - 2) + 1(x - 2) &= 0 \\ (3x + 1)(x - 2) &= 0 \end{aligned}$$